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TARGET: A MODEL FOR DETERMINING HITS ON AN IRREGULARLY SHAPED TARGET

Fred L. Bunn Sue B. Hinman

February 1985

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US ARMY BALLISTIC RESEARCH LABORATORY
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INTRODUCTION

This report documents a Fortran 77 program for finding whether a projectile hits an irregularly shaped target. It discusses input preparation, tells about the various levels of output provided, and describes the mathematics used by the program. The input and output sections give a sample case which may be used for testing the program. A copy of the program is included in the appendix.

This program determines whether a projectile hits a complex target and if desired, which faces were entered or exited. The target may be composed of one or more polyhedra. As examples, the target could be several tanks, a hollow box, or a donut shaped polyhedron. Restricting the target to polyhedra is not a severe limitation because solids with curved surfaces may be represented to any desired accuracy by increasing the number of polygonal faces. Currently, the model handles targets with up to 20 corners and 20 faces but this is easily increased by changing the three parameter statements in the program.

INPUT DATA

To obtain successful results the input data must be prepared in a specific order. If the order is not followed exactly, the output data will be incorrect. First make sure you have numbered all of the corners and faces of your polygon. The polygons used in this program must be convex polygons. This is not really a limitation as a concave polygon may be broken down into several convex polygons. The coordinate system used in this program is in three dimensions so that the x axis is traveling East, the y axis North, and the z axis Up.

Line 1 should contain the level number. If level=1, the program simply prints whether the target was hit or not. If level=2, it prints an input echo and tells which faces were entered or exited. And, if level=3, it prints the input echo, the results of intermediate calculations, and which faces were entered or exited, if any. DO NOT place a decimal point after the number.

Line 2 should contain the coordinates of the projectile's velocity. The three coordinates (x,y,z) should be placed next to each other horizontally and separated by either commas and/or spaces. The x coordinate should be first, followed by the y, and then the z. DO place a decimal point after the numbers.

Line 3 should contain the coordinates of the projectile. They should be based on the aim point of the projectile to the target. They should be entered exactly like the velocity coordinates in the line above. DO place a decimal point after the numbers.

Line 4 should be the number of corners. The program is set to allow up to 20 corners on the target, so be sure that your number is less than or equal to 20. DO NOT place a decimal point after the number.

Lines 5-n are for the coordinates of the corners. Each corner's coordinates should be entered like those of the projectile's velocity. Corner number one's coordinates will be on the first of these, line number two's on the next, and so forth until you are completed. DO NOT leave any blank lines after these. DO make sure that the number on line four is the same as the number of sets of corner coordinates. DO place a decimal point after the numbers.

Line n+1 should contain the number of faces the target has. The program is set to allow up to 20 faces on the target, so check the number before trying to run the program. DO NOT place a decimal point after the number.

Lines n+2 and following will contain the numbers of the corners for each of the faces, one face per input line. The numbers of the corners should be read in a clockwise direction around the edge of the face starting from any corner on the face. The program allows for six corners per face. If a face has less than six corners just fill in the extra spaces with zeros. Make sure the faces are listed in order as you have numbered them. Face number one should be in the first row, two in the second, and so forth until you have completed them. DO NOT place a decimal point after the numbers. When you have completed your input file you may check it with the sample below to double check your accuracy. The right hand column tells you what is found in each row.

Figure 1 shows a tank turret corresponding to the data in Table 1.

OUTPUT DATA

The program generates output in three levels of detail depending on the first input value. You may select the level you think is most appropriate for your immediate purposes. Level one simply prints whether the target was hit or not. Level two prints an input echo and tells which faces were entered or exited. Level three prints the input echo, the results of intermediate calculations, and which faces were entered or exited, if any.

Level one prints one of the following messages:

Yes, it was hit.

No, it was not hit.

TABLE 1. SAMPLE INPUT FOR A TANK TURRET

Sar	Sample Input Data					
As seen in file	Explanation					
1	level of output datail					
3., 4., 0.	beginning velocity coordinates					
-2., 0., 1.	beginning projectile coordinates					
12	number of corners					
.9, -4.3, 1.5	coordinates of corners					
.9, -5.3, 0.	Ħ					
9, -4.3, 1.5	H					
9, -5.3, 0.	an.					
-3.7,-3.2,1.5	п					
-4.8, -3.9, 0.	n					
-3.7, 6.2, 1.5	п					
-4.8, 7.5, 0.	п					
3.7, 6.2, 1.5	п					
4.8, 7.5, 0.	п					
3.7, +2., 1.5	п					
4.8, +2.7, 0.	п					
8	number of faces					
1, 2, 4, 3, 0, 0	number of each corner in					
3, 4, 6, 5, 0, 0	the face going in a					
5, 6, 8, 7, 0, 0	clockwise direction					
7, 8, 10, 9, 0, 0	п					
9, 10, 12, 11, 0, 0	п					
11, 12, 2, 1, 0, 0	π					
1, 3, 5, 7, 9, 11	tf .					
2, 4, 6, 8, 10, 12	tf					

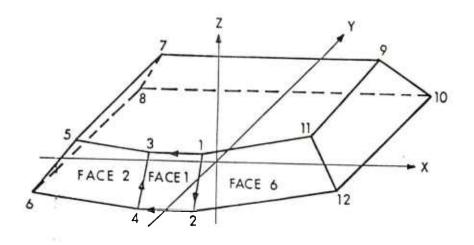


Figure 1. A Tank Turret

Level two on the other hand will produce a moderate amount of output data. With your input data being echoed you may do another check to make sure the data are all correct so that the solution that is printed is correct. If the target is not hit it simply will not print which faces were entered and exited. A sample level two output looks like this:

TABLE 2. SAMPLE	OUTPUT FOR	PRINT LEVE	EL TWO		
,	ж	У	Z		
Projectile velocity	3.000	4.000	.000		
Projectile position	-2.000	.000	1.000		
Positions of the 12 co	rners:				
	.900	-4.300	1.500		
	.900	-5.300	.000		
	900	-4.300	1.500		
	900	-5.300	.000		
	-3.700	-3.200	1.500		
	-4.800	-3.900	.000		
	-3.700	6.200	1.500		
	-4.800	7.500	.000		
3.700 6.200 1.500					
4.800 7.500 .000					
	-2.000	1.500			
	4.800	-2.700	.000		
Corners of the 8 face	8:				
1 2	4	3	0	0	
3 4	6	5	0	0	
3 4 5 6 7 8	8	7	0	0	
7 8	10	9	0	0	
9 10	12	11	0	0	
11 12	2	1	0	0	
1 3	5	7	9	11	
2 4	6	8	10	12	
Projectile entered thr	u face 3				
Projectile exited thr	u face 4				

Level three contains the maximum amount of data output. If doing any work that involves very specific data, you should use level three. It prints all of the same output as in level two plus the new projectile position after rotation, the new corner coordinates after rotation and translation, the number of corners in each face, the corner numbers with their vector coordinates, and the associated edge numbers, vectors, and cross products. Just like level two, level three will not print which faces were entered and exited if the target was not hit. A sample level three output would look like this:

TABLE 3. SAMPLE OUTPUT FOR PRINT LEVEL THREE

			x	y	z				
Projectile vel	oci	ty	3.000	4.000	.000				
Projectile pos			-2.000	.000	1.000				
Positions of t									
			.900	-4.300	1.500				
			.900	-5.300	.000				
			900	-4.300	1.500				
			900	-5.300	.000				
			-3.700	-3.200	1.500				
			-4.800	-3.900	.000				
			-3.700	6.200	1.500				
			-4.800	7.500	.000				
			3.700	6.200	1.500				
			4.800	7.500	.000				
			3.700	-2.000	1.500				
			4.800	-2.700	.000				
Corners of the	Ę		es:						
1		2	4	3	0		0		
3		4	6	5	0		0		
5		6	8	7	0		0		
7		8	10	9	0		0		
9		10	12	11	0		0		
11		12	2	1	0		0		
1		3	5	7	9		11		
2		4	6	8	10		12		
New projectile	_		-1.600	-1.200	1.000				
New corner pos	it;	ons							
			4.900	-2.900	.500				
			5.500	-3.700	-1.000				
			3.460	-3.980	.500				
			4.060	-4.780	-1.000				
			.560	-4.780	.500				
			.100	-6.000	-1.000				
			-5.080	2.740	.500				
			-6.740	3.120	-1.000				
			.840	7.180	.500				
			.940	8.880	-1.000				
			5.760	.620	.500				
Para 4 has li			7.060	.720	-1.000				
Face 1 has 4				2 000	F00				
Corner vector	_	is:	3.460	-3.980	.500	00000	ا د داد ه سو	2	200
Edge vector Corner vector		is:	1.440 4.900	1.080		cross	product	1S:	.720
Edge vector		is:	.600	-2.900 800	-1 500	oncos	nno du st	10.	7 650
Corner vector		is:	5.500	-3.700	-1.500	GROSS	product	TS:	7.650
Edge vector		is:	-1.440	-1.080		orose	product	10.	1.440
Corner vector		is:	4.060	-4.780	-1.000	01000	pr oduct	10.	1.440
Edge vector		is:	600	.800		orose	product	10.	-5.490
Tabe 10001	ر	*D.	000	.000	1.500	01 022	product	13:	- 3.490

TABLE 3 CONTD.

Face 2 has 4	CO	ners.							
Corner vector		is:	.560	-4.780	.500				
Edge vector	3	is:	2.900	.800		cross	product	is:	1.450
Corner vector	3	is:	3.460	-3.980	.500			,	,0
Edge vector	4	is:	.600	800		cross	product	is:	5.490
Corner vector	4	is:	4.060	-4.780	-1.000		P. 0 0 0 0 0		J. 190
Edge vector	6	is:	-3.960	-1.220	.000	cross	product	is:	3.960
Corner vector	6	is:	.100	-6.000	-1.000				5.700
Edge vector	5	is:	.460	1.220	1.500	cross	product	is:	610
Face 3 has 4	co	rners.					•		
Corner vector	7	is:	-5.080	2.740	.500				
Edge vector	5	is:	5.640	-7.520	.000	cross	product	is:	2.820
Corner vector	5	is:	.560	-4.780	.500				
Edge vector	6	is:	460	-1.220	-1.500	cross	product	is:	.610
Corner vector	6	is:	.100	-6.000	-1.000		•		
Edge vector	8	is:	-6.840	9.120	.000	cross	product	is:	6.840
Corner vector	8	is:	-6.740	3.120	-1.000		•		
Edge vector	7	is:	1.660	380	1.500	cross	product	is:	8.450
Projectile ent			face 3				•		_
Face 4 has 4	COI	rners.							
Corner vector	9	is:	.840	7.180	.500				
Edge vector	7	is:	-5.920	-4.440	.000	cross	product	is:	-2.960
Corner vector	-	is:	-5.080	2.740	.500				
Edge vector		is:	-1.660	.380	-1.500	cross	product	is:	-8.450
Corner vector		is:	-6.740	3.120	-1.000				
Edge vector		is:	7.680	5.760	.000	cross	product	is:	-7.680
Corner vector			. 940	8.880	-1.000				
Edge vector		is:	100	-1.700	1.500	cross	product	is:	-1.310
Projectile exi			face 4						
Face 5 has 4									
Corner vector			5.760	.620	.500				
Edge vector	-	is:	-4.920	6.560		cross	product	is:	-2.460
Corner vector	_	is:	.840	7.180	.500				
Edge vector		is:	.100	1.700	-1.500	cross	product	is:	1.310
Face 6 has 4									
Corner vector		is:	4.900	-2.900	.500				
_		is:	.860	3.520	.000	cross	product	is:	. 430
Corner vector			5.760	.620	.500				
		is:	1.300	.100		cross	product	is:	9.290
Corner vector			7.060	.720	-1.000				
Edge vector		is:	-1.560	-4.420		cross	product	is:	1.560
Corner vector		is:	5.500	-3.700	-1.000				
Edge vector	1	is:	600	.800	1.500	cross	product	is:	-7.650

TABLE 3 CONTD.

Face 7 has 6	COI	rners.							
Corner vector	11	is:	5.760	.620	.500				
Edge vector	1	is:	860	-3.520	.000	cross	product	is:	430
Corner vector	1	is:	4.900	-2.900	.500				
Edge vector	3	is:	-1.440	-1.080	.000	cross	product	is:	720
Corner vector	3	is:	3.460	-3.980	.500				
Edge vector	5	is:	-2.9 00	800	.000	cross	product	is:	-1.450
Corner vector	5	is:	.560	-4.780	.500				
Edge vector	•	is:	-5.640	7.520	.000	cross	product	is:	-2.820
Corner vector	•	is:	-5.080	2.740	.500				
Edge vector	-	is:	5.920	4.440	.000	cross	product	is:	2.960
Face 8 has 6		rners.							
Corner vector	12	is:	7.060	.720	-1.000				
Edge vector	2	is:	-1.560	-4.420	.000	cross	product	is:	1.560
Corner vector	2	is:	5.500	-3.700	-1.000				
Edge vector		is:	-1.440	-1.080	.000	cross	product	is:	1.440
Corner vector	-	is:	4.060	-4.780	-1.000				
Edge vector	_	is:	- 3.960	-1.220	.000	cross	product	is:	3.960
Corner vector	6	is:	.100	-6.000	-1.000				
Edge vector	8	is:	-6.840	9.120	.000	cross	product	is:	6.840
Corner vector	8	is:	-6.740	3.120	-1.000				
Edge vector	10	is:	7.680	5.760	.000	cross	product	is:	-7.680

MATHEMATICS

This section describes the inner workings of the program. The program is divided into three parts related as shown in Figure 2. The MAIN routine is simply a driver program that reads inputs, echoes them as desired, and calls the two subsidiary routines. The XFORM subroutine rotates the target and translates it to a new coordinate system such that the projectile is traveling up the new y axis and passes through the origin. The HIT TGT function takes these new coordinates and examines each face to find if the projectile passes through that face.

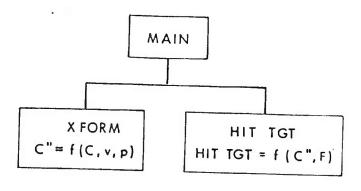


Figure 2. Program Heirarchy

Data Requirements

The coordinates are assumed to form a right-handed coordinate system and may be thought of as an x-axis positive toward the East, a y-axis positive toward the North, and a z-axis positive upward. Angles are measured from the y-axis clockwise.

The projectile is assumed to be in the vicinity of the target with a known position \vec{p} , and known velocity \vec{v} . The vertical or z component of the velocity vector is assumed to be zero. The target is assumed to be one or more polyhedra with convex faces, and is assumed to be described by its n corners in a matrix C of n rows and 3 columns. If a face is concave, it can be judiciously divided into several convex polygons when input is prepared. It is further assumed that each face has 3 to 6 corners and that the corners of the n faces are listed in a matrix F with n rows and 6 columns. The nth row contains a list of the m corners clockwise around the nth face as one looks from the outside of the polyhedron. If m is less than 6, the remaining elements of the row are zeroes.

Transformation of Target and Projectile Coordinates

The first step is to transform the coordinates of the target to a new coordinate system such that the projectile is traveling up the y-axis. The XFORM routine uses \vec{p} , \vec{v} , and C to produce a new matrix C' which is the transformed matrix of corners, with the vector of each corner on a separate row. For the projectile and each corner vector, the rotation is equivalent and is as follows:

$$c_{x'}' = c_{x} \cos \theta + c_{y} \sin \theta$$

$$c_{y'}' = -c_{x} \sin \theta + c_{y} \cos \theta$$

$$c_{z'}' = c_{z}$$

where $\theta = -atan(v_y, v_z)$, \vec{c} is the original vector and c' is the vector after rotation.

Figure 3 illustrates the rotation and subsequent translation. The equations for the translation are:

$$c_{s'}{}' = c_{s'} - p_{s'}$$

 $c_{z'}{}' = c_{z'} - p_{z'}$
 $c_{y'}{}' = c_{y'}$

In practice, the program uses the C matrix directly to produce a C' matrix rather than using \overline{c} , $\overline{c'}$, and $\overline{c'}$ vectors for the individual rows.

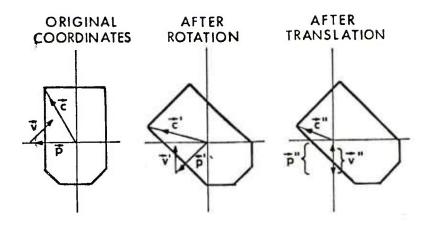


Figure 3. Transformation of Target Coordinates

Hit Determination

The HIT TGT function uses the C' matrix, and the F pointer matrix to find whether the target is hit. To do this, the program examines the silhouettes of the faces. If the sides of a silhouette encompass the origin of the coordinate system, the face is hit, but not otherwise. Figure 4 shows two silhouettes; the one on the left is hit and the one on the lower right is missed.

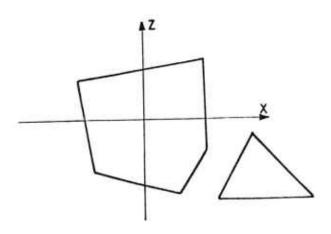


Figure 4. Target Faces Hit or Missed

To find whether a face is hit, the program examines the edges of its silhouette in turn. It uses the F pointer matrix to strip the two corners associated with an edge out of the C' matrix and place them in \overline{c} , and \overline{c}' (not to be confused with vectors of the same name used in the XFORM subroutine.) Assume that \overline{c} , is a corner of the silhouette, \overline{c}' is the corner immediately clockwise, and \overline{c} is a vector representing the edge between these two corners. Then, as shown in Figure 5,

$$\vec{e} = \vec{c}' - \vec{c}$$
.

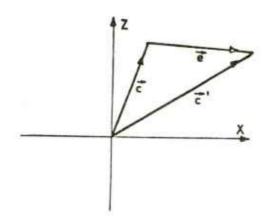


Figure 5. Edge and Corner Vectors

Now for \vec{c} , \vec{c} , the cross product will be a vector along the y axis. Notice that if the y component of the result is positive, the projectile can hit the silhouette because both the projectile (i.e. the origin) and the silhouette lie on the right of \vec{c} , that is, they are in the same half-plane. If the result is negative, however, the origin and the silhouette lie on opposite sides of the edge and no hit is possible. Mathematically, a hit is possible if and only if $r_u > 0$, where

$$r_y = c_z e_z - c_z e_z .$$

If all the cross products for the edges are positive in y, then the face is entered. Notice that a face on the far side of the target has its corners ordered clockwise when viewed from the outside of the target, but when viewed from the inside or behind, they are counter-clockwise. This allows us to find which faces are exited; they will be the faces whose cross products are all negative.

In summary, if a face has all positive cross products, it is entered; if a face has all negative cross products, it is exited; and if the cross products are a mixture of positive and negative, it is not hit. If we just want to know whether a target is entered, we examine each face until a negative cross product is found and examine faces until we find one that is hit. Notice also that we can determine whether an unclosed polyhedron is hit if we check both entries and exits.

Mechanization of the Algorithm

The correspondence between the notation discussed in this algorithm and that used in the actual program is shown in Table 2.

TABLE 4. CORRESPONDENCE BETWEEN ALGORITHM AND PROGRAM NOTATIONS

NOTATION USED IN						
	Algorithm	Program				
	C	corner				
XFORM	C''	cornr2				
subroutine	p	p				
	₹	v				
	c	c				
HIT TGT	ē	e				
function	у	у				
	F	faces				
	C'	cornr2				

In actual practice, the y column of the C, and C' matrices is never used because for the silhouettes all values are zero.

SUMMARY

The program is a elegant algorithm for determining hits on irregular targets. It will find whether a hit occurs, and if desired, which faces are entered and exited. The target may be any open or closed polyhedron or a set of polyhedra. The elegance is due in part to the algorithm's careful organization and its ability to look at a single edge of a face and often determine that the projectile does not enter the face.

There are several modifications that could be made to this model. The ability to handle projectiles that are ascending or descending is a possible modification. The model could also be modified to find the angle at which the projectile strikes the faces. The structure makes it easy to take the two subsidiary routines and include them in larger combat models or to take the XFORM subroutine alone and use it to find silhouettes for other purposes. It can also be easily changed to run faster if only the faces entered are considered.

APPENDIX: PROGRAM LISTING

```
parameter (NN=20)
     PURPOSE: Find whether a projectile strikes a polyhedral target
С
     logical hit tgt, hit
     common /comtgt/ corner(NN,3), iface(NN,6), ncorns, nfaces
     common /projec/ v(3), p(3), lev
     real cornr2(NN,3)
1
     format(26x,'x
2
     format(' Projectile velocity', 3f10.3)
3
     format(' Projectile position',3f10.3)
4
     format(' Positions of the',i3,' corners:')
5
     format(' Corners of the', 13, ' faces:')
6
     format(20x,3f10.3)
7
     format(6110)
С
     Read inputs
         read *,lev
         read , v
         read *, p
         read *, ncorns
         read #, ((corner(i, j), j=1,3), i=1, ncorns)
         read *, nfaces
         read *,((iface(i, j), j=1,6),i=1, nfaces)
     IF (lev.gt.1) THEN
         print 1
         print 2, v
         print 3,p
         print 4, ncorns
         print 6, ((corner(i, j), j=1,3),i=1,ncorns)
         print 5, nfaces
         print 7,((iface(i, j), j=1,6),i=1, nfaces)
     ENDIF
     call xform(cornr2)
     hit = hit tgt(cornr2)
     END
С
     LOGICAL FUNCTION HIT TGT (cornr2)
С
     C
     Purpose: Find whether target is hit
     parameter (NN=20)
     logical hit' fac
     common /comtgt/ corner(NN,3), iface(NN,6), ncorns, nfaces
     common /projec/ v(3), p(3), lev
     dimension c(3), e(3), cornr2(NN,3)
     format(' Corner vector', i3, 'is:',3f10.3)
1
2
     format(' Edge vector ',i3,' is:',3f10.3,' cross product is:',f10.3)
```

```
format(' Face', i3, ' has', i2, ' corners.')
3
c
     hit tgt=.false.
     Check each face to see if it was hit
C
     DO 50 n=1, nfaces
         hit fac=.false.
         Find j, the number of corners of face n
C
          D0 20 k=1.6
              IF (iface (n,k) .gt. 0) j=j+1
          CONTINUE
20
          if (lev.eq.3) print 3,n,j
         k=iface(n, j)
         nneg = 0
         npos = 0
         Check each edge to see if the polygon and origin are in the
C
         same half plane.
C
         DO 30 l=1,j
          Load corner vector
C
               e(1) = cornr2(k, 1)
               c(2) = cornr2(k, 2)
               c(3) = cornr2(k,3)
               if (lev.eq.3) print 1,k,c
          Load edge vector
               k=iface(n,1)
               e(1) = cornr2(k, 1) - c(1)
               e(2) = cornr2(k, 2) - c(2)
               e(3) = cornr2(k,3) - c(3)
           y=e(1)*c(3)-c(1)*e(3)
           if (lev.eq.3) print 2,k,e,y
           if (y . lt. 0) nneg = nneg + 1
           if (y . gt. 0) npos = npos + 1
           if ((nneg .ge. 1) .and. (npos .ge. 1)) GOTO 40
30 .
         CONTINUE
40
         CONTINUE
         if (npos.eq.j .or. nneg.eq.j) hit fac = .true.
         IF (lev.gt.1 .and. hit fac) THEN
           if (nneg.eq.j) print*,'Projectile exited thru face',n
           if (npos.eq.j) print*, 'Projectile entered thru face', n
         ENDIF
         hit tgt=hit tgt .or. hit fac
          if (lev .eq. 1 .and. hit tgt) GO TO 60
     CONTINUE
50
60
     CONTINUE
     if (lev.eq.1 .and. hit tgt) print*, 'Yes, it was hit.'
     if (.NOT. hit tgt) print*, 'No, it was not hit.'
     END
```

C

```
SUBROUTINE XFORM(cornr2)
C
C
     PURPOSE: Rotate and translate target, proj to proj base coords
     parameter (NN=20)
     common /comtgt/ corner(NN,3), iface(NN,6), ncorns, nfaces
     common /projec/ v(3), p(3), lev
     dimension cornr2(NN.3)
     format(' New projectile pos:',3f10.3)
1
     format(' New corner positions are:')
2
3
     format(20x,3f10.3)
C
С
     Find sin, cos of rotation angle
         factor = 1./sqrt(v(1)**2 + v(2)**2)
         sina = -v(1)*factor
         cosa = v(2) *factor
     Rotate projectile position
C
         xp = p(1)*cosa + p(2)*sina
         yp =-p(1)*sina + p(2)*cosa
         if (lev.eq.3) print 1, xp, yp, p(3)
C
     Rotate & translate coordinates of target corners
         DO 20 nc=1, ncorns
          cornr2(nc,1) = corner(nc,1)*cosa + corner(nc,2)*sina - xp
          cornr2(nc,2) = -corner(nc,1)*sina + corner(nc,2)*cosa
          cornr2(nc,3) = corner(nc,3) - p(3)
20
         CONTINUE
         if (lev.eq.3) print 2
         if (lev.eq.3) print 3,((cornr2(i,j),j=1,3),i=1,ncorns)
```

END

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